1. Conservative and Active Currency Strategies. Performance Attribution

Forward Surprise

Foreign currency risk premium is the difference between the percentage change in the spot exchange rate and the forward premium (or discount)

(1)
$$r_c = r_d - f = \frac{S_t - F}{S_0}$$

This premium is also referred as the forward contract return or the forward surprise.

Unhedged position

If the currency exposure is unhedged the discrete return on a foreign asset translated into home currency units can be written as

(2)
$$r_N = (1 + r_z)(1 + r_d) - 1$$

where

 r_z – the foreign asset return,

 r_d – the percentage change in the spot exchange rate using the home currency/foreign currency convention.

The approximate unhedged return to the domestic investor is

$$(3) r_{N} \approx r_{z} + r_{d}$$

The continuously compounded return would be

(4)
$$ln(1+r_N) = ln(1+r_z) + ln(1+r_d)$$
 or $r_N^* = r_z^* + r_d^*$

Consider an investment in US T-bills with one year maturity and yield to maturity equal to $r_z = i_{\rm f}^{\rm N}$. Forward premium is approximately equal to the difference between domestic risk-free rate and foreign risk-free rate.

$$(5) f \approx \left(i_d^N - i_f^N\right)$$

The approximate unhedged return to the domestic investor is

(6)
$$r_N \approx i_f^N + r_d = i_d^N + r_d - f = i_d^N + r_c$$

The unhedged return is equal to

- foreign risk-free rate plus currency return (percentage change in the exchange rate), or
- domestic risk-free rate plus the foreign currency risk premium (forward surprise).

Hedged position

The currency exposure in a foreign asset may be hedged by selling a forward contract. The hedged return on the foreign asset will be equal to:

(7)
$$r_H = r_N + h(r_d - f)$$

where

r_N – unhedgd return,

h – hedge ratio,

 r_d - f – forward contract return.

The hedge ratio (h) is the coefficient indicating what portion of the total exposure should be hedged. The negative hedge ratio (h) refers to short (selling) position, while the positive hedge ratio is used to indicate long (buying) position in the derivative instrument (forward or futures contract). A long currency position or positive currency gap may be hedged by selling forward or futures contracts (negative hedge ratio). A short currency position may be hedged by buying forward or futures contracts (positive hedge ratio). Such convention is also very useful when a currency portfolio consists of many assets and derivatives including currency options. The sign of the hedge ratio indicates what an investor should do (sell or buy).

To hedge the principal and the interest, the hedge ratio should be equal to $h = -(1+r_z*T)$. When T=1 the fully hedged foreign asset return is approximately equal to asset return plus forward premium. The exact return is equal to

(8)
$$r_H = (1 + r_z)(1 + r_d) - 1 - (1 + r_z)(r_d - f) = (1 + r_z)(1 + f) - 1$$

When we add arbitrage relationship (covered interest arbitrage) the hedged return is

(9)
$$r_{H} = (1 + r_{z})(1 + f) - 1 = (1 + r_{z})\frac{F}{S_{0}} - 1 = (1 + r_{z})\frac{(1 + i_{d}^{N})}{(1 + i_{f}^{N})} - 1$$

In addition we may assume that the long currency position consists of risk-free rate foreign government securities ($r_z = i_f^N$), and we have

$$(10) r_{\rm H} = i_{\rm d}^{\rm N}$$

The fully hedged return on the risk-free investment abroad is equal to the domestic risk-free rate.

The hedged return on the long currency position hedged by selling a forward contract is

(11)
$$r_H = (1 + r_z)(1 + r_d) - 1 + h(r_d - f) \approx r_z + r_d + h(r_d - f)$$

where

 r_z – the foreign asset return,

 $r_d\!-\!the$ percentage change in the spot exchange rate using the home currency/foreign currency convention,

h – hedge ratio,

f – forward premium.

The hedge ratio h may be replaced with the currency exposure ratio H (H=1+h). The last indicates the proportion of the total currency asset exposure left unhedged. When the currency exposure is unhedged H=1, when the currency exposure is fully hedged H=0

With the currency exposure ratio the hedged return is equal to:

(12)
$$r_H \approx r_z + r_d + (H-1)(r_d - f) = r_z + f + H(r_d - f)$$

When H=1 (unhedged position) return is equal to the asset return plus the unknown future currency return

$$(13) r_{N} \approx r_{z} + r_{d}$$

When H=0 (fully hedged position) return is equal to the asset return plus the forward premium (both of them are known are known in advance)

(14)
$$r_H \approx r_z + f$$

The relationship between the unhedged return and the hedged return are presented in the following figure

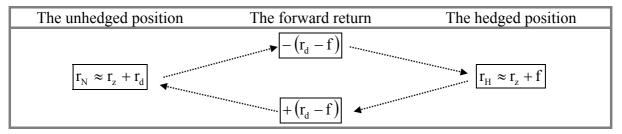


Figure 1. The unhedged and hedged currency position

Optimization of return on hedged currency position

The optimization model may have the following objective function

(15)
$$E(r_z) + f + H[E(r_d) - f] - \alpha (\sigma_{r_z}^2 + H^2 \sigma_{r_d}^2 + 2H \rho_{r_z r_d} \sigma_{r_z} \sigma_{r_d})$$

where

 $E(r_{x})$ - expected foreign asset return,

f – the currency forward premium or discount,

 $E(r_d)$ – f expected return of the forward contract ("forward surprise"),

 $E(r_d)$ - expected currency return,

H – currency exposure ratio,

 α - risk aversion penalty,

 σ_r^2 - variance of foreign asset return,

 $\sigma_{\rm r.}^2$ - variance of the currency return,

 $\rho_{\rm r_z r_d} \sigma_{\rm r_z} \sigma_{\rm r_d}$ - covariance between the foreign asset return and the currency return,

 $ho_{\mathrm{r_zr_d}}$ - correlation coefficient between the foreign asset return and the currency return.

The objective function maximizes risk adjusted currency portfolio return. Currency risk is measured by the variance of portfolio return.

Problem 1. The unhedged and hedged position with forward, options and FX swap

A bank invests \$10 million in the US T-bills with 1 year maturity. Yield to maturity is 5%.

The spot exchange rate is 4,00 PLN/USD. The domestic risk-free rate is 12%.

The foreign risk-free rate is 5%.

(a) Calculate the unhedged return when foreign exchange rate is changed by +- 10%, 20%, 30%?

(b) Calculate the hedged return when the position is hedged with a forward contract.

Calculate the forward exchange rate.

What are the profits/losses against the unhedged position?

Compare the hedged return with a domestic risk-free return.

(c) Calculate the hedged return for a covered call and protective put strategies.

The exercise exchange rate is 4,00 PLN/USD, standard deviation is 10%.

Option prices are established using BSM model.

(d) Show the currency hedging using FX swap with a 1 year maturity.

What capital transactions may replicate the FX swap?

Solution

(a)

Situation in t=0

Exposure in foreign currency 9,524 million USD
Spot exchange rate 4,00 PLN/USD
Exposure in domestic currency 38,095 million PLN

Unhedged position in t=1

Curency return r _d	-30,0%	-20,0%	-10,0%	0,0%	10,0%	20,0%	30,0%
Exposure in foreign currency	10,000	10,000	10,000	10,000	10,000	10,000	10,000
Spot exchange rate (t=1)	2,80	3,20	3,60	4,00	4,40	4,80	5,20
Value of the unhedged position	28,000	32,000	36,000	40,000	44,000	48,000	52,000
The unhedged return	-26,5%	-16,0%	-5,5%	5,0%	15,5%	26,0%	36,5%
Return on foreign asset r _z	5,0%	5,0%	5,0%	5,0%	5,0%	5,0%	5,0%
Currency return r _d	-30,0%	-20,0%	-10,0%	0,0%	10,0%	20,0%	30,0%
The unhedged return $(1+r_z)(1+r_d)-1$	-26,5%	-16,0%	-5,5%	5,0%	15,5%	26,0%	36,5%
The approximate unhedged return $= r_z + r_d$	-25,0%	-15,0%	-5,0%	5,0%	15,0%	25,0%	35,0%

(b) **Hedged position with a forward contract**Forward exchange rate 4,2667

Time t=1

-30,0%	-20,0%	-10,0%	0,0%	10,0%	20,0%	30,0%
10,000	10,000	10,000	10,000	10,000	10,000	10,000
4,27	4,27	4,27	4,27	4,27	4,27	4,27
42,667	42,667	42,667	42,667	42,667	42,667	42,667
12.0%	12.0%	12 0%	12 0%	12 0%	12.0%	12,0%
12,070	12,070	12,070	12,070	12,070	12,070	12,070
14 667	10 667	6 667	2 667	_1 333	-5 333	-9,333
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					-14,0%	-24,5%
-30,0%	-20,0%	-10,0%	0,0%	10,0%	20,0%	30,0%
6,7%	6,7%	6,7%	6,7%	6,7%	6,7%	6,7%
26.70/	26.70/	16 70/	(70/	2.20/	12 20/	22.20/
-30,7%	-20,7%	-10,/%	-0,7%	3,3%	13,3%	23,3%
-1,05	-1,05	-1,05	-1,05	-1,05	-1,05	-1,05
38,5%	28,0%	17,5%	7,0%	-3,5%	-14,0%	-24,5%
-26,5%	-16,0%	-5,5%	5,0%	15,5%	26,0%	36,5%
12,0%	12,0%	12,0%	12,0%	12,0%	12,0%	12,0%
11,7%	11,7%	11,7%	11,7%	11,7%	11,7%	11,7%
-5,0%	-5,0%	-5,0%	-5,0%	-5,0%	-5,0%	-5,0%
1,8%	1,3%	0,8%	-	-	-0,7%	-1,2%
13,5%	13,0%	12,5%	12,0%		11,0%	10,5%
-1,5%	-1,0%	-0,5%	0,0%	0,5%	1,0%	1,5%
-10,095	-6,095	,	,	_	9,905	13,905
	-10,159	-6,349	-2,540	-	5,079	8,889
4,571	4,571	4,571	4,571	4,571	4,571	4,571
	10,000 4,27 42,667 12,0% 14,667 38,5% -30,0% 6,7% -36,7% -1,05 38,5% -26,5% 12,0% 11,7% -5,0% 1,8% 13,5% -1,5% -13,968	10,000 10,000 4,27 4,27 42,667 42,667 12,0% 12,0% 14,667 10,667 38,5% 28,0% -30,0% -20,0% 6,7% 6,7% -1,05 -1,05 38,5% 28,0% -26,5% -16,0% 12,0% 12,0% 11,7% 11,7% -5,0% -5,0% 1,8% 1,3% 13,5% 13,0% -1,5% -1,0% -10,095 -6,095 -13,968 -10,159	4,27 4,27 4,27 42,667 42,667 42,667 12,0% 12,0% 12,0% 14,667 10,667 6,667 38,5% 28,0% 17,5% -30,0% -20,0% -10,0% 6,7% 6,7% 6,7% -36,7% -26,7% -16,7% -1,05 -1,05 -1,05 38,5% 28,0% 17,5% -26,5% -16,0% -5,5% 12,0% 12,0% 12,0% 11,7% 11,7% 11,7% 1,8% 1,3% 0,8% 13,5% 13,0% 12,5% -1,5% -1,0% -0,5% -10,095 -6,095 -2,095 -13,968 -10,159 -6,349	10,000 10,000 10,000 10,000 4,27 4,27 4,27 4,27 42,667 42,667 42,667 42,667 12,0% 12,0% 12,0% 12,0% 14,667 10,667 6,667 2,667 38,5% 28,0% 17,5% 7,0% -30,0% -20,0% -10,0% 0,0% 6,7% 6,7% 6,7% 6,7% -36,7% -26,7% -16,7% -6,7% -1,05 -1,05 -1,05 -1,05 38,5% 28,0% 17,5% 7,0% -26,5% -16,0% -5,5% 5,0% 12,0% 12,0% 12,0% 12,0% 11,7% 11,7% 11,7% 11,7% 11,7% 11,7% 11,7% 11,7% -5,0% -5,0% -5,0% -5,0% 1,8% 1,3% 0,8% 0,3% 13,5% 13,0% 12,5% 12,0% -1,5% -1,0% -0,5% 0,0% -1,5% -1,0% -0,5%	10,000 10,000 10,000 10,000 10,000 4,27 4,27 4,27 4,27 42,667 42,667 42,667 42,667 12,0% 12,0% 12,0% 12,0% 14,667 10,667 6,667 2,667 -1,333 38,5% 28,0% 17,5% 7,0% -3,5% -30,0% -20,0% -10,0% 0,0% 10,0% 6,7% 6,7% 6,7% 6,7% 6,7% -36,7% -26,7% -16,7% -6,7% 3,3% -1,05 -1,05 -1,05 -1,05 38,5% 28,0% 17,5% 7,0% -3,5% -26,5% -16,0% -5,5% 5,0% 15,5% 12,0% 12,0% 12,0% 12,0% 12,0% 11,7% 11,7% 11,7% 11,7% 11,7% -5,0% -5,0% -5,0% -5,0% -5,0% -1,8% 1,3% 0,8% 0,3% -0,2% 13,5% 13,0% 12,5% 12,0% 11,5% <tr< td=""><td>10,000 10,000 10,000 10,000 10,000 10,000 10,000 4,27 4,27 4,27 4,27 4,27 4,27 4,27 42,667 42,667 42,667 42,667 42,667 42,667 42,667 12,0% 12,0% 12,0% 12,0% 12,0% 12,0% 14,667 10,667 6,667 2,667 -1,333 -5,333 38,5% 28,0% 17,5% 7,0% -3,5% -14,0% -30,0% -20,0% -10,0% 0,0% 10,0% 20,0% 6,7% 6,7% 6,7% 6,7% 6,7% 6,7% -36,7% -26,7% -16,7% -6,7% 3,3% 13,3% -1,05 -1,05 -1,05 -1,05 -1,05 -1,05 38,5% 28,0% 17,5% 7,0% -3,5% -14,0% -26,5% -16,0% -5,5% 5,0% 15,5% 26,0% 12,0% 12,0% 12,0% 12,0% 12,0% 12,0% 11,7% 11,7% 11,7%</td></tr<>	10,000 10,000 10,000 10,000 10,000 10,000 10,000 4,27 4,27 4,27 4,27 4,27 4,27 4,27 42,667 42,667 42,667 42,667 42,667 42,667 42,667 12,0% 12,0% 12,0% 12,0% 12,0% 12,0% 14,667 10,667 6,667 2,667 -1,333 -5,333 38,5% 28,0% 17,5% 7,0% -3,5% -14,0% -30,0% -20,0% -10,0% 0,0% 10,0% 20,0% 6,7% 6,7% 6,7% 6,7% 6,7% 6,7% -36,7% -26,7% -16,7% -6,7% 3,3% 13,3% -1,05 -1,05 -1,05 -1,05 -1,05 -1,05 38,5% 28,0% 17,5% 7,0% -3,5% -14,0% -26,5% -16,0% -5,5% 5,0% 15,5% 26,0% 12,0% 12,0% 12,0% 12,0% 12,0% 12,0% 11,7% 11,7% 11,7%

(c) **Hedging - Short CALL**

Premium is calculated using BSM model Sensitivity measures

0,3097 PLN/USD									
Gamma	Theta	Rho	Vega						
0,79	0,00	0,03	0,01						

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Curency return r _d	-30,0%	-20,0%	-10,0%	0,0%	10,0%	20,0%	30,0%
Profit - premium received	3,097	3,097	3,097	3,097	3,097	3,097	3,097
Loss, when the foreign exchange rate in time t=1 is above the strike price	0,000	0,000	0,000	0,000	-4,000	-8,000	-12,000
Profit / Loss from Short CALL	3,097	3,097	3,097	3,097	-0,903	-4,903	-8,903
Value of the unhedged position	28,000	32,000	36,000	40,000	44,000	48,000	52,000
Value of the hedged position	31,097	35,097	39,097	43,097	43,097	43,097	43,097
The unhedged return	-18,4%	-7,9%	2,6%	13,1%	13,1%	13,1%	13,1%
Total gains							
ΔS	-10,095	-6,095	-2,095	1,905	5,905	9,905	13,905
ΔC	-3,097	-3,097	-3,097	-3,097	0,903	4,903	8,903
$\Delta V = \Delta S + h\Delta C$	-6,998	-2,998	1,002	5,002	5,002	5,002	5,002

Delta

0,77

Delta-neutral hedge ratio h=- $\Delta I/\Delta_c$

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Curency return r _d	-30,0%	-20,0%	-10,0%	0,0%	10,0%	20,0%	30,0%
Profit - premium received	4,004	4,004	4,004	4,004	4,004	4,004	4,004
Loss, when the foreign exchange rate in time t=1 is above the strike price	0,000	0,000	0,000	0,000	-5,172	-10,344	-15,516
Profit / Loss from Short CALL	4,004	4,004	4,004	4,004	-1,168	-6,340	-11,512
Value of the unhedged position	28,000	32,000	36,000	40,000	44,000	48,000	52,000
Value of the hedged position	32,004	36,004	40,004	44,004	42,832	41,660	40,488
The unhedged return	-16,0%	-5,5%	5,0%	15,5%	12,4%	9,4%	6,3%
Total gains							
ΔS	-10,095	-6,095	-2,095	1,905	5,905	9,905	13,905
ΔC	-3,097	-3,097	-3,097	-3,097	0,903	4,903	8,903
$\Delta V = \Delta S + h\Delta C$	-6,091	-2,091	1,909	5,909	4,737	3,565	2,393

Hedging - Long PUT

Premium is calculated using BSM model Sensitivity measures

0,0525 PLN/USD

Delta	Gamma	Theta	Rho	Vega
-0,23	0,79	0,00	-0,01	0,01

Equal-dollar hedge ratio				1			
Curency return r _d	-30,0%	-20,0%	-10,0%	0,0%	10,0%	20,0%	30,0%
Loss - premium paid	-0,525	-0,525	-0,525	-0,525	-0,525	-0,525	-0,525
Loss, when the foreign exchange rate in time t=1 is below the strike price	12,000	8,000	4,000	0,000	0,000	0,000	0,000
Profit / Loss from Long Put	11,475	7,475	3,475	-0,525	-0,525	-0,525	-0,525
Value of the unhedged position	28,000	32,000	36,000	40,000	44,000	48,000	52,000
Value of the hedged position	39,475	39,475	39,475	39,475	43,475	47,475	51,475
The unhedged return	3,6%	3,6%	3,6%	3,6%	14,1%	24,6%	35,1%
Total gains							
ΔS	-10,095	-6,095	-2,095	1,905	5,905	9,905	13,905
ΔΡ	11,475	7,475	3,475	-0,525	-0,525	-0,525	-0,525
$\Delta V = \Delta S + h\Delta P$	1,380	1,380	1,380	1,380	5,380	9,380	13,380

Delta-neutral hedge ratio h=- $\Delta I/\Delta_p$

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Curency return r _d	-30,0%	-20,0%	-10,0%	0,0%	10,0%	20,0%	30,0%
Loss - premium paid	-2,315	-2,315	-2,315	-2,315	-2,315	-2,315	-2,315
Loss, when the foreign exchange rate	52,950	35,300	17,650	0,000	0,000	0,000	0,000
in time t=1 is below the strike price	50.626	22.096	15 225	2 215	2 215	2 215	2 215
Profit / Loss from Long Put Value of the unhedged position	50,636 28,000	32,986 32,000	15,335 36,000			-2,315 48,000	-2,315 52,000
Value of the unnedged position Value of the hedged position	78,636	,	′ ′	,	,	45,685	49,685
The unhedged return	106,4%	,	*			19,9%	30,4%
Total gains	,		,	,			
ΔS	-10,095	-6,095	-2,095	1,905	5,905	9,905	13,905
ΔΡ	11,475	7,475	3,475	-0,525	-0,525	-0,525	-0,525
$\Delta V = \Delta S + h\Delta P$	40,540	26,890	13,240	-0,410	3,590	7,590	11,590

(d)

	Rate	t=0	t=1	Capital transactions
Take a loan, million USD	5%	9,524	10,000	issue securities
Make a deposit, million PLN	12%	38,095	42,667	buy domestic T-bill
FX rate (PLN/USD		4,000	4,267	

Performance Attribution

Measuring performance attribution for actively managed portfolios is theoretically simple. The total value added from active management can be calculated by comparing the portfolio's return with the portfolio's benchmark return. Decomposition of the value added into components to determine sources of increase or decline in value is more difficult. The sources of value added may decomposed to

- active asset management (selection of foreign assets),
- asset allocation (structure of foreign assets),
- currency allocation (selection of foreign currencies).

Two techniques of the performance attribution used in practice include

- absolute contribution analysis,
- relative contribution analysis.

Both techniques identify the contribution of the above stated sources of value added to the performance of a currency portfolio and both compare the realized return with the benchmark portfolio. If the currency portfolio in time t=1 is compared to the currency portfolio in time t=0 the decomposition of value added does not show in detail the whole history of contribution. Both techniques give the same results, but they partition the same value added in different way.

The realized total currency portfolio return is

(16)
$$r_{p} = \sum_{i} w_{i} [r_{z}^{i} + f_{i}] + \sum_{j} H_{j} [r_{d}^{j} - f_{j}]$$

where

 \boldsymbol{w}_{i} - the portfolio weight held in asset i,

 r_z^i - the asset return of asset i,

f_i - the forward premium for currency i,

H_i - the currency exposure of the portfolio to currency j,

 r_d^j - the currency return for currency j.

The return on the benchmark portfolio (all elements are with $\,^\sim$ sign) can be calculated as

(17)
$$\widetilde{\mathbf{r}}_{\mathbf{p}} = \sum_{i} \widetilde{\mathbf{w}}_{i} \left[\widetilde{\mathbf{r}}_{\mathbf{z}}^{i} + \mathbf{f}_{i} \right] + \sum_{j} \widetilde{\mathbf{H}}_{j} \left[\mathbf{r}_{d}^{j} - \mathbf{f}_{j} \right] = \widetilde{\mathbf{r}}_{\mathbf{p}}^{z} + \widetilde{\mathbf{r}}_{\mathbf{p}}^{d}$$

where

(18)
$$\widetilde{\mathbf{r}}_{p}^{z} = \sum_{i} \widetilde{\mathbf{w}}_{i} \left[\widetilde{\mathbf{r}}_{z}^{i} + \mathbf{f}_{i} \right]$$
 - the required (benchmark) hedged asset return,

(19)
$$\widetilde{r}_{p}^{d} = \sum_{j} \widetilde{H}_{j} [r_{d}^{j} - f_{j}]$$
 - the benchmark return for the currency j.

Let the difference between the realized asset return and the benchmark asset return be

(20)
$$\Delta r_z^i = r_z^i - \widetilde{r}_z^i$$

We can also write the changes in portfolio weights and currency exposure as

(21)
$$\Delta w_i = w_i - \widetilde{w}_i$$

(22)
$$\Delta H_i = H_i - \widetilde{H}_i$$

Absolute contribution analysis decomposes the value added (more exactly the difference between the total portfolio return and the total benchmark portfolio return) in the following way

$$\begin{split} &(23) \quad r_{p} - \widetilde{r}_{p} = \sum_{i} w_{i} \Delta r_{z}^{i} + \sum_{i} \Delta w_{i} \big[\widetilde{r}_{z}^{i} + f_{i} \big] + \sum_{j} \Delta H_{j} \big[r_{d}^{j} - f_{j} \big] + \varepsilon \\ &\sum_{i} w_{i} \Delta r_{z}^{i} \qquad \quad \text{- active asset management,} \\ &\sum_{i} \Delta w_{i} \big[\widetilde{r}_{z}^{i} + f_{i} \big] \qquad \quad \text{- active asset allocations,} \\ &\sum_{j} \Delta H_{j} \big[r_{d}^{j} - f_{j} \big] \qquad \quad \text{- active currency allocation.} \end{split}$$

The last error term ϵ captures the cross-products between asset returns and currency returns and is relatively small.

Active asset management gives positive value added when selected assets including financial instruments have higher returns than the assets in the benchmark portfolio. It is reasonable to select assets with greater returns but it is also important to keep in mind that higher return of asset is accompanied by greater credit risk. The conservative policy (selection of credit risk-free government securities) will produce tiny results.

Active asset allocation evaluates the changes in the structure of portfolio. The best results are obtained when the weights of the highest hedged returns are increased.

Active currency allocation involves selection of currencies and the appropriate currency exposures which is obtained using the hedge ratios and derivatives. The value added depends on hedge ratios and also the forward contract return. The last component depends on currency returns which are not dependent on a company wishes or decisions. But a conservative company using regularly hedged currency positions (H=0, Δ H=0) may almost completely eliminate profits and losses from the currency allocation.

Relative contribution analysis represents an alternative way of measuring the same value added. The active asset management component is not changed. But this technique changes the way the individual value added by active asset allocation and active currency allocation. These values are calculated using the aggregate benchmark return for assets and the aggregate benchmark return for currencies. Such rearrangement changes the individual returns. The value added is

$$(24) \qquad r_{_{P}}-\widetilde{r}_{_{P}}=\sum_{_{i}}w_{_{i}}\Delta r_{_{z}}^{^{i}}+\sum_{_{i}}\Delta w_{_{i}}\Big[\widetilde{r}_{_{z}}^{^{i}}+f_{_{i}}-\widetilde{r}_{_{P}}^{^{z}}\Big]+\sum_{_{j}}\Delta H_{_{j}}\Big[r_{_{d}}^{^{j}}-f_{_{j}}-\widetilde{r}_{_{P}}^{^{d}}\Big]+e$$

Problem 2. The currency performance attribution

Consider the performance of a simple portfolio composed of domestic bonds (position 1) and three investments in three different currencies (positions 2, 3, and 4).

Realized	Strategy

Realized Strategy						
Position	1	2	3	4		
The local asset return	of asset i				•	
r i	2,00%		1,00%	5,00%		
The currency return for	r currency	, j			•	
$r_d^{\ j}$		-1,00%	2,00%	3,00%		
The forward premium	for curren	icy i			•	
f_i		0,10%	0,10%	0,10%		
The currency exposure	e of the po	rtfolio to	currenc	уj	•	
H_{j}		-0,50	0,10	0,50		
The portfolio weights	held in ass	set i			•	
W_i	40%	10%	20%	30%		
The realized return for	the hedge	ed assets				
$w_{i} \left[r_{z}^{i} + f_{i} \right]$	0,80%	0,01%	0,22%	1,53%	$\sum_i w_i \Big[r_z^i + f_i \Big]$	2,56%
The ralized return for	the curren	cy				
$H_{j}\left[r_{d}^{j}-f_{j}\right]$		0,55%	0,19%	1,45%	$\sum_{j} H_{j} \left[r_{d}^{j} - f_{j} \right]$	2,19%
Total return	0,80%	0,56%	0,41%	2,98%	r _P =	4,75%
The Benchmark Stat	egy					
The local asset return	of asset i					
$\widetilde{r}_{\!\scriptscriptstyle z}^{\mathrm{i}}$	1,00%	1,00%	1,00%	1,00%		
The currency exposure	e of the po	rtfolio to)			
$\widetilde{\mathrm{H}}_{\mathrm{j}}$		-0,10	0,10	0,10		

The portfolio weights				
$\widetilde{\mathrm{w}}_{\mathrm{i}}$	25,0%	25%	25,0%	25,0%

The benchmark return for the assets

$\widetilde{\mathbf{w}}_{i} \left[\widetilde{\mathbf{r}}_{z}^{i} + \mathbf{f}_{i} \right]$	0,25% 0,28%	0,28% 0,28%	$\left \widetilde{r}_{p}^{z} = \sum_{i} \widetilde{w}_{i} \left[\widetilde{r}_{z}^{i} + f_{i} \right] \right $	1,08%
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The benchmark return for the currency

$\widetilde{H}_{j} \left[r_{d}^{j} - f_{j} \right]$		0,11%	0,19%	0,29%	$\widetilde{r}_{p}^{d} = \sum_{j} \widetilde{H}_{j} \left[r_{d}^{j} - f_{j} \right]$	0,59%
Total return	0,25%	0,39%	0,47%	0,57%	$\widetilde{r}_p =$	1,67%

Total value added $r_p - \tilde{r}_p = 3,09\%$

- (a) Show the absulute contribution analysis results.
- (b) Show the relative contribution analysis results.

RISK MANAGEMENT [6352-02]

Solution

(a)

Absulute Contribution Analysis

Active	asset management	

$w_i \Delta r_z^i$ 0,40% -	-0,10%	$1,20\%$ $\sum_{i} w_{i} \Delta r_{z}^{i}$	1,50%
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Active asset allocation

Active currency allocation

$\Delta H_{j} \left[r_{d}^{j} - f_{j} \right]$	0,44%	1,16%	$\sum_{j} \Delta H_{j} \left[r_{d}^{j} - f_{j} \right]$	1,60%
	<u> </u>			

Total value added	0,55%	0,18%	-0,06%	2,42%	$r_{p}-\widetilde{r}_{p}=$	3,09%
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(b)

Relative Contribution Analysis

Active asset management

$w_i \Delta r_z^i$ 0,40% -0,10%	$1,20\%$ $\sum_{i} w_{i} \Delta r_{z}^{i}$	1,50%
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Active asset allocation

$\left[\Delta w_i \left[\widetilde{r}_z^i + f_i - \widetilde{r}_p^z \right] \right]$	-0,01% 0,00%	0,00% 0,00	$0\% \left[\sum_{i} \Delta w_{i} \left[\widetilde{r}_{z}^{i} + f_{i} - \widetilde{r}_{p}^{z} \right] \right]$	-0,02%
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Active currency allocation

$\DeltaH_{j}\Big[r_{d}^{\;j}-f_{j}-\widetilde{r}_{p}^{\;d}\Big]$		0,68%		0,92%	$\sum_{j} \Delta H_{j} \left[r_{d}^{j} - f_{j} - \widetilde{r}_{p}^{d} \right]$	1,60%
Total value added	0,39%	0,57%	0,00%	2,13%	$r_P - \widetilde{r}_P =$	3,09%