

## 12. Long-Term Debt. Term Structure of Interest Rates. Leasing

**Problem 63**

Is a bond selling at a discount or a premium if the annual coupon interest rate is 10% and the market requires a return of 8% ? How much is an investor willing to pay for this bond if it matures in 5 years ?

**Solution**

Bond Value 1079,9

Since the coupon rate exceeds the discount rate, the bond is priced at a premium.

|     |     |     |     |       |
|-----|-----|-----|-----|-------|
| 1   | 2   | 3   | 4   | 5     |
| 100 | 100 | 100 | 100 | 1 100 |

NPV = 1 079,9

**Problem 64**

A bond has a par value \$100 and fixed annual coupon rate 10%.

Yield to maturity is 8% and maturity is 5 years.

(a) Calculate the price of a bond at the end of  $t=0$ .

(b) Calculate the price at the end of the first year before and after interest payment.

What is the possible range for a bond price in the first year when YTM does not change ?

(c) Calculate the price of a bond 90 days later. Assume that YTM is 12% at that time.

**Solution**

(a)

The bond price at the end of  $t=0$ :

$$P_0 = \frac{10\% \times 100}{(1+8\%)^1} + \frac{10\% \times 100}{(1+8\%)^2} + \frac{10\% \times 100}{(1+8\%)^3} + \frac{10\% \times 100}{(1+8\%)^4} + \frac{10\% \times 100 + 100}{(1+8\%)^5} = 107,99$$

The price of a bond is equal to the sum of discounted cash flows (interests + principal repayment).

| Period               | 1      | 2      | 3      | 4      | 5      |
|----------------------|--------|--------|--------|--------|--------|
| Cash flow            | 10     | 10     | 10     | 10     | 110    |
| Discounting factor   | 0,9259 | 0,8573 | 0,7938 | 0,7350 | 0,6806 |
| Discounted cash flow | 9,26   | 8,57   | 7,94   | 7,35   | 74,86  |
| Cumulated cash flow  | 9,26   | 17,83  | 25,77  | 33,12  | 107,99 |

(b)

After one year and interest payment the price of bond is equal to the sum of discounted four interest payments and repayment of the par value at maturity.

$$P_1 = \frac{10\% \times 100}{(1+8\%)^1} + \frac{10\% \times 100}{(1+8\%)^2} + \frac{10\% \times 100}{(1+8\%)^3} + \frac{10\% \times 100 + 100}{(1+8\%)^4} = 106,62$$

Price after interest payment

106,62

Interests

10,00

Price before interest payment

116,62

Assuming that YTM is the the same the discounted price of  $t=1$  is equal to the price at  $t=0$ .

$$P_0 = \frac{116,2}{(1+8\%)} = 107,99$$

The price of a bond should be in the range of (107,99; 116,62).

(c)

After 90 days, there is 275 days to the first interest payment. This is a 0,753 fraction of a year.

Maturity is equal 4,753 years. The price of a bond is:

$$P = \frac{10}{(1+0,12)^{0,753}} + \frac{10}{(1+0,12)^{1,753}} + \frac{10}{(1+0,12)^{2,753}} + \frac{10}{(1+0,12)^{3,753}} + \frac{110}{(1+0,12)^{4,753}} = 95,42$$

Clean price

92,96 using Excel

Accrued interests

2,47 = 10% \* 100 \* 90 / 365

Dirty price

95,42

| Period               | 0,753  | 1,753  | 2,753  | 3,753  | 4,753  |
|----------------------|--------|--------|--------|--------|--------|
| Cash flow            | 10     | 10     | 10     | 10     | 110    |
| Discounting factor   | 0,9182 | 0,8198 | 0,7320 | 0,6535 | 0,5835 |
| Discounted cash flow | 9,18   | 8,20   | 7,32   | 6,54   | 64,19  |
| Cumulated cash flow  | 9,18   | 17,38  | 24,70  | 31,23  | 95,42  |

**Problem 65**

A company is considering the acquisition of 10 personal computers. The computers can be purchased for \$3500 each and would be depreciated straight line over 5 years. Their estimated final value at the end of 5 years is \$0. The purchase may be financed with a loan. Before-tax cost of debt is 14%. The tax rate is 40%. Alternatively, the 10 computers can be leased for \$10000 annually, payable at the end of each year.

- (a) Calculate the sum of discounted cashflows (PV) when the company purchases computers.
- (b) Calculate the sum of discounted cashflows (PV) when the company leases computers.
- (c) Show the sensitivity of PV to interest rate.

**Solution**

(a)

Purchase. Cash flows = loan payment - tax saving:

| Year | Loan Payment | Interest   | Principal | Loan Balance | Depreciation | Expense | Tax Saving | Cash Flows |
|------|--------------|------------|-----------|--------------|--------------|---------|------------|------------|
| 0    |              |            |           | 35000,0      |              |         |            |            |
| 1    | 10194,9      | 4900,0     | 5294,9    | 29705,1      | 7000,0       | 11900,0 | 4760,0     | 5434,9     |
| 2    | 10194,9      | 4158,7     | 6036,2    | 23668,9      | 7000,0       | 11158,7 | 4463,5     | 5731,4     |
| 3    | 10194,9      | 3313,6     | 6881,3    | 16787,6      | 7000,0       | 10313,6 | 4125,5     | 6069,5     |
| 4    | 10194,9      | 2350,3     | 7844,7    | 8942,9       | 7000,0       | 9350,3  | 3740,1     | 6454,8     |
| 5    | 10194,9      | 1252,0     | 8942,9    | 0,0          | 7000,0       | 8252,0  | 3300,8     | 6894,1     |
|      |              | $\Sigma =$ | 35000,0   |              |              |         | PV =       | 23 937,3   |

(b)

Leasing. Cash flows = after tax lease payment

| Year | Lease Payment | After Tax Lease Payment |
|------|---------------|-------------------------|
| 1    | 10000,0       | 6000,0                  |
| 2    | 10000,0       | 6000,0                  |
| 3    | 10000,0       | 6000,0                  |
| 4    | 10000,0       | 6000,0                  |
| 5    | 10000,0       | 6000,0                  |
|      |               | PV = 23 705,8           |

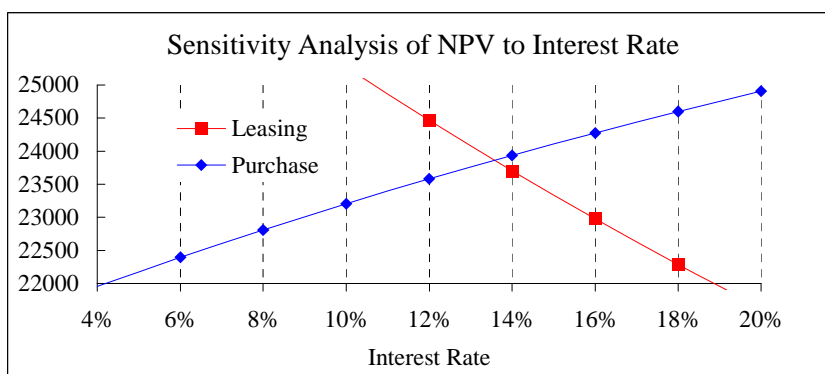
PV of expenses

|          |                 |
|----------|-----------------|
| Purchase | 23 937,3        |
| Leasing  | <u>23 705,8</u> |
|          | 231,5           |

It is better to lease.

(c)

|     | Leasing | Purchase |
|-----|---------|----------|
|     | 23706   | 23937    |
| 4%  | 27955   | 21954    |
| 6%  | 27014   | 22394    |
| 8%  | 26121   | 22810    |
| 10% | 25274   | 23205    |
| 12% | 24470   | 23581    |
| 14% | 23706   | 23937    |
| 16% | 22979   | 24276    |
| 18% | 22287   | 24599    |
| 20% | 21629   | 24907    |



**Problem 66**

A leasing company has just received an order from a client who wishes to lease 10 computers for 5 years. The leasing company can buy computers for \$3500 each. It will depreciate them straight line to a salvage value \$0 in five years. It will finance this project with debt. Before-tax cost of debt is 13,33%. Lease payments will be received at the end of each year and are subject to taxation immediately upon receipt. The leasing company is in the 40% tax bracket.

(a) Calculate lease payment required to breakeven the leasing company expenses.  
 (b) Calculate lease payment if required NPV for a leasing company is equal to \$135,8.

**Solution**

(a)

Discount rate (after-tax cost of debt): 8%

Investment cost is \$35 000. Annual tax saving is  $35000 / 5 \times 40\% = 2800$ .

First, we calculate the present value of tax savings:

|                        | 1     | 2     | 3     | 4     | 5     |       |
|------------------------|-------|-------|-------|-------|-------|-------|
| Tax savings            | 2 800 | 2 800 | 2 800 | 2 800 | 2 800 |       |
| Discounting factor     | 0,93  | 0,86  | 0,79  | 0,74  | 0,68  | PV    |
| Discounted tax savings | 2593  | 2401  | 2223  | 2058  | 1906  | 11180 |

Next, we find the annual after-tax lease payment that gives the PV equal to \$23820.

Lease payment can be calculated with the PMT function:  $PMT(8\%;5;-23820,4;;0) = \$5966$ .

The before-tax lease payment should be \$9943,3.

The present value of tax savings and lease payments will be equal to zero.

|                    | 0        | 1      | 2      | 3      | 4      | 5      |     |
|--------------------|----------|--------|--------|--------|--------|--------|-----|
| Investment         | -35000   |        |        |        |        |        |     |
| Tax savings        |          | 2 800  | 2 800  | 2 800  | 2 800  | 2 800  |     |
| Lease payments     |          | 5 966  | 5 966  | 5 966  | 5 966  | 5 966  |     |
| Cash Flows         | -35 000  | 8 766  | 8 766  | 8 766  | 8 766  | 8 766  |     |
| Discounting factor | 1,0000   | 0,9259 | 0,8573 | 0,7938 | 0,7350 | 0,6806 | PV  |
| DCF                | -35000,0 | 8116,6 | 7515,4 | 6958,7 | 6443,3 | 5966,0 | 0,0 |

(b)

Now we have to find lease payment which gives the present value equal to  $23820,4 + 135,8 = \$23956,3$ .Lease payment can be calculated with the PMT function:  $PMT(8\%;5;-23956,3;;0) = \$6000$ .

The before-tax lease payment should be \$10000,0.

The present value of tax savings and lease payments will be equal to \$135,8.

|                    | 0        | 1      | 2      | 3      | 4      | 5      |       |
|--------------------|----------|--------|--------|--------|--------|--------|-------|
| Investment         | -35000   |        |        |        |        |        |       |
| Tax savings        | 0        | 2 800  | 2 800  | 2 800  | 2 800  | 2 800  |       |
| Lease payments     |          | 6 000  | 6 000  | 6 000  | 6 000  | 6 000  |       |
| Cash Flows         | -35 000  | 8 800  | 8 800  | 8 800  | 8 800  | 8 800  |       |
| Discounting factor | 1,0000   | 0,9259 | 0,8573 | 0,7938 | 0,7350 | 0,6806 | PV    |
| DCF                | -35000,0 | 8148,1 | 7544,6 | 6985,7 | 6468,3 | 5989,1 | 135,8 |